

Characteristics of in-based carbide include its structural, mechanical, electrical, optical, and thermodynamic properties

Ramulu, Ravi Kumar
Assistant Professor, Assistant Professor,
Department of Humanities and Science, S
amskruti College of Engineering and Techology, Ghatkesar

Abstract:

Through the use of first-principles calculations based on the density functional theory, we were able to investigate the structural, mechanical, electrical, optical, and thermodynamic aspects of antiperovskite compounds $M_3\text{InC}$ (where $M=Y$ and La) (DFT). According to the experimental results, the optimised lattice parameters are in excellent agreement. The elastic property that was noticed The constants are all positive, demonstrating the mechanical stability of all of these stages. Cauchy pressure, Pugh's ratio, and Poisson's ratio are all measures of pressure. The brittleness features of these compounds should be shown. For each of these stages, it is expected that there would be dislocation movement. The Peierls stress was used to corroborate this. In the case of $M_3\text{InC}$ (where $M=Y$ and La), the anisotropy factor calculated by Zener reveals the anisotropic behaviour. The bulk modulus and hardness values of Y_3InC and La_3InC demonstrate the softening behaviour of the materials. The investigation of the band structure In addition to diagrams, the density of states (both the total density of states and the partial density of states) demonstrate metallic behaviour for all of the elements. compounds. The strong reflectivity of Y_3InC and La_3InC in the high energy range (8-9 eV) shows that these materials are attractive candidates for future applications. In the UV energy area, there is a coating substance. The absorption and conductivity spectra reveal that the absorptivity and conductivity of the sample are both excellent. the visible and ultraviolet (UV) spectrums We have also looked at the Debye temperature, minimum thermal conductivity, and melting temperature. These compounds' temperature may be calculated from their elastic constants.

1. Introduction

Antiperovskite $M_3\text{BX}$ crystals, which are composed of a unique sort of stable perovskite structure with a high number of ternary phases, are the hottest of all the materials studied so far. From the perspective of crystallography, The cubic structure of the $M_3\text{BX}$ crystal structure is related to the cubic structure of Cu_3Au . The formula $M_3\text{BX}$ contains the atoms M and B , which are coincident. In the middle of the face and at eight corners, connecting with twelve nearby atoms whereas X and Y coincide in the centre of the body [1], respectively. as a result of The capacity to adjust it gives birth to a variety of technological devices. By varying the electron configuration, the same structure may be achieved. Density is a topic that receives a great deal of attention in the contemporary period. opened the door to a new vista There is a lot more to it than that. the possibility of exploring it because of its attractive physical characteristics able to meet the demands of the present day Scientists have been working on new discoveries in recent years. Some fascinating characteristics of a stable chemical were discovered. The antiperovskite structure is composed of a compound having the formula $M_3\text{BX}$. As a result, it has been noticed that some individuals Ti_3AlN , for example, is an antiperovskite molecule having this structure. [2, Ti_3AlC [3, Sc_3AlC [4, Sc_3AlC [5, Sc_3AlN [6, Sc_3InN [7] are examples of exhibits. Mechanical qualities that are satisfactory. Furthermore, emphasis was placed on Investigate the possibilities of ferromagnetism or ferromagnetic resonance. Several materials, such as Ni_3GaC [7], exhibit superconductivity. Ni_3MgC , Ni_3CdC [8], Ni_3InC [9], Cr_3GaN , and Cr_3RhN [10] are

examples of transition metal compounds examined. Among the M_3AC compounds with A that have been studied with the exception of Ni_3CdC (which has Tc), none of the other elements are superconductors. = 3.4 kilocalories [11]

In comparison, several significant results demonstrate that antiperovskite is effective. Compared to nitride, metal-carbide exhibits a number of intriguing properties. Owing to the presence of carbon-containing material as an impurity, it is projected to a considerable degree of ductility and strength [12]. In addition, the hardness is a factor. When C was introduced, the property of binary TiAl improved as well. [13, 14] increased up to 11 GPa. As a result, dealing with metal-carbide metal alloy is a method of creating more advanced materials with better strength. Physical and mechanical qualities provide a number of advantages. On the other hand, the M_3BX structure makes use of all of the available resources. A and B were created by substituting items from groups ii and iv. Position and features of the objects are also determined [1]. As a result, it's intriguing to look for fresh materials to investigate difficult issues. Understanding the insight mechanism of the A_3InC structure is a challenging challenge. With the addition of a new element to a website a piece of writing about the paper M_3InC ($M=Y, La$) has been published, in which they demonstrate the [15] The preparation of the substance Finding the right one is often difficult. The optical and electrical characteristics of such materials undergo drastic modifications. substance, while rare earth elements are replaced in the A-site on the other hand The A_3BX structure is used. Once again, the responsiveness, fragility, and other characteristics Experimentally concealed physical and mechanical features are discovered investigations conducted under the tremendous pressure of a sample of this calibre That is to say In this scenario, theoretical analysis is one of the most important methods of clarifying fundamental issues. knowledge of macroscopic phenomena by the use of such material phenomenon.

First-principles calculations were performed on La antiperovskite in order to study the involvement of Y and La in the M_3InC structure. Despite the fact that these sorts of antiperovskites have been explored by a large number of researchers, M_3InC crystal structures have been discovered, however no previous work has been discovered on this compound. crystal structures have not been discovered yet. Methods of Computational Analysis The researches based on basic principles have been carried out. CASTEP is based on density functional theory (DFT) [16] and is used.

PerdewBurke-Ernzerhof (PBE) exchange correlation energy function is used in the GGA approximations to code [17] inside the GGA approximations. It has been proposed that the electron-ion interactions are described by Pseudo-potentials of the Vanderbilt type that are ultrasoft [19]. The aircraft took off and landed safely. A wave energy cut-off of 500 eV was used to both stages of the experiment to reduce wave energy. Extend the range of the wave functions. Both of these structures have similar structural properties. Phases have been examined using the BFGS system [20] in conjunction with a bare minimum of energy Brillouin zone sampling has been carried out using the Monkhorst-Pack grid [21], which consists of 9 9 9 kpoints. The The 1 10⁻⁵ rule was used to establish convergence criteria. eV/atom of energy the total energy, 0.03 eV/m of severe force, and 0.05 GPa of total pressure Maximum displacement is 0.001 inch and the tension is 0.001 inch. The elastic is a good example of this. The determination of stiffness constants for both phases has been carried out utilising an approach based on stress-strain relationships [22]. The Debye temperatures of both were measured. Compounds have been estimated based on data from the elastic constant.

3. Discussion of the Findings

3.1 Structural characteristics of the materials

The carbides antiperovskites M_3InC (where $M=Y$ and La) are a kind of antiperovskites. The cubic crystal structure with pm m (No. 221) space has been discovered. group, and each unit cell has 5 atoms. The Wyckoff positions in the case of These carbides antiperovskites have the following atom

configurations: M: (0, 0.5, 0.5), In: (0, 0.5, 0.5), (0, 0, 0) and the letter C (0.5, 0.5, 0.5). M₃InC's crystal structure is shown below. Figure 1 depicts the equation (where M=Y and La).

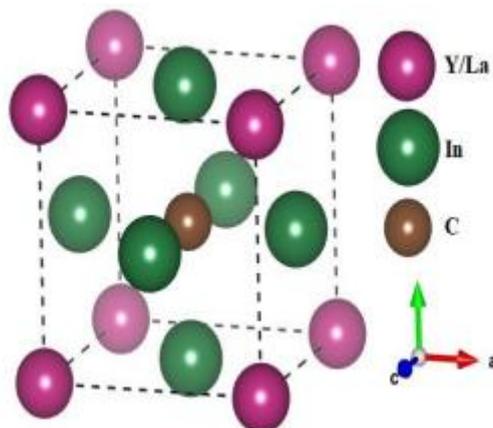


Fig 1: Crystal structure of M₃InC (where M=Y and La).

By minimizing the energy and force convergence, we have calculated the structural parameters. The calculated structural parameters such as lattice parameter a_0 , cell volume V_0 and bulk modulus B_0 are presented in Table 1 with the available experimental data [15]. The optimized lattice parameters evident a good agreement with experimental data with some deviations. These deviations occurred by the temperature dependence lattice parameters and GGA process [23]. Also the over estimation of the lattice parameters are the common

Table 1: Calculated lattice parameter a_0 (Å), cell volume V_0 (Å³) and bulk modulus B_0 of M₃InC (where M=Y and La).

Compound	a_0			V_0	B_0
	This work	Expt. [1]	Deviation (%)		
Y ₃ InC	4.995	4.902	1.897	124.625	100.861
La ₃ InC	5.299	5.193	2.04	148.793	58.107

3.2 Elastic properties

Elastic constants are critical parameters in the formation of a molecule. These are used to evaluate the qualities of a compound's stability, stiffness, ductility, brittleness, and anisotropy, among other things. There are a number of them. The elastic constants are just three and they are independent of one another. Specifically, for cubic carbide antiperovskites M₃InC (where M=Y and La), the elastic constants of M₃InC have been determined by the use of At time zero, the stress-strain function according to Hook's law [24] is observed. K and P are equal to 0 GPa. The second order elastic constants have been discovered and quantified. The bulk modulus, Young's modulus, and shears are all calculated using this formula. M₃InC's modulus, Pugh's ratio, and Poisson's ratio are all measured. We have what we need. In addition, the Cauchy's pressure CP and the Zener's pressure ZP were determined. The estimated elastic constants have an anisotropy index of A . C_{ij} , a large amount Young's modulus E , Cauchy's modulus B , shear modulus G , Young's modulus B The pressure CP , the Pugh's ratio B/G , the Poisson's ratio ν , and the Zener's ratio are all measurements of pressure. Table 2 shows predictions for the anisotropy index A of M₃InC. Moreover, the elastic constants C_{ij} of M₃InC are positive and meet the Born condition. requirements for long-term stability $C_{11}-C_{12}>0$, $C_{44}>0$, and $C_{11}+2C_{12}>0$ [25] are all possible combinations. demonstrating the mechanical stability of the M₃InC material under investigation For The value of B in our two compounds is greater than the value of G ,

which also exists. The mechanical stability of M₃InC is shown by the number 26. Both stress and anxiety are a part of everyday life. Young's modulus, often known as tensile strength, is a measure of strain ratio. E is the modulus. The value of E is obtained by dividing 9BG by (3B+G). The stiffness behaviour of the compound is determined by this parameter. The vast majority of people The greater the value of E, the greater the stiffness qualities of a material. [27] is a compound. As a result, Y₃InC is more rigid than La₃InC. Petti calculated the Cauchy's pressure CP = C₁₂-C₄₄ for [28] and came to the conclusion that Solids' brittleness and ductility are described in this way. The unfavourable positive value of Cauchy's pressure indicates the presence of brittle material. Characteristics of a compound that are (ductile). The brittle/ductile distinction Pugh's B/G ratio [29] may also be used to understand the properties. [29] as well as the Poisson's ratio $\nu = (3B-E)/6G$ [30]. The high monetary worth of The Pugh's ratio (B/G > 1.75) and the Poisson's ratio ($\nu > 0.26$) both indicate that The ductility of a compound is increased when the value is low (B/G 1.75). The compound will be fragile if the values of $\nu < 0.26$ are used. in accordance with Cauchy's pressure CP, Pugh's ratio B/G, and Poisson's ratio ν are all measures of pressure. Both compounds exhibit brittleness properties when subjected to the same conditions. study. It is also shown that Y₃InC has a higher degree of brittleness. La₃InC has different features from La₃InC. The crucial parameter that determines the strength of a crystal is its density. The Peierls stress of dislocations, also known as the Peierls stress of dislocations, may be computed using The following equations may be used to calculate the shear modulus G and the Poisson's ratio ν : [equation]]

$$\sigma_p = \frac{2G}{1-\nu} \exp\left(-\frac{2\pi d}{b(1-\nu)}\right) \quad (1)$$

The electronic characteristics of a substance

The electrical characteristics of materials are critical in distinguishing them as either metals, semiconductors, or insulators [36]. In this inquiry, we have computed the band of interest. Y₃InC and La₃InC crystal structures, as well as whole and partial Y₃InC There is a high density of states. The results of the computed band configurations have shown as seen in Fig. 2. The band structures in the X-R-M-R spectrum have been investigated. In the first Brillouin zone, there is a high symmetry point. In addition, the Energy band structures have been estimated within a range of -9 to 6 eV. range. The dotted horizontal line between the valence band and the base band. Consider the Fermi level, which is the conduction band at zero energy. The The band structures demonstrate that certain sub-bands have crossed the main band. Fermi level at R and points for Y₃InC, as well as at R and points for Y₃InC. La₃InC. Thus, we infer that the band structures have been modified. There is no band gap between the two bands (valence and conduction). For As a result of the above, we determine that both documents disclose Nature's metallic sheen The total and partial densities of the computed total and partial density of In Fig. 3, the states have been shifted. The valence bands of the total valence The density of states exhibits a first peak at around -14 eV and a second peak at approximately -14 eV. For Y₃InC, lengthy peaks are mostly caused by In 4d states, which are rare. The The second shot type peak appears at around -8.5 eV, which further increases the energy. It results from the combination of C 2s and Y 4d (or La 5d) states A Between the long and short wavelengths, prohibited energy gaps of roughly -3 eV are seen. as well as brief peaks The third peak has an energy of around -5 eV. Another prohibited energy gap between -8 and -5 eV has been discovered. a variety of energy levels This is the range of energy between -4 eV and Fermi level. This is mostly due to the interaction of the C 2p and Y 4d states. the presence of an admixture In the fourth dimension. The conduction band of total density is defined as follows:

The distribution of states exhibits two peaks that are further elevated for the With the addition of C 2p states, the contribution of Y 4d (or La 5d) states increases.

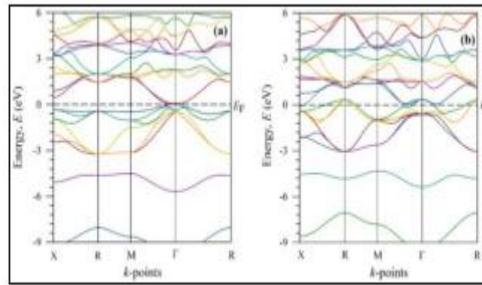


Fig 2: Electronic band structure of (a) Y3InC and (b) La3InC.

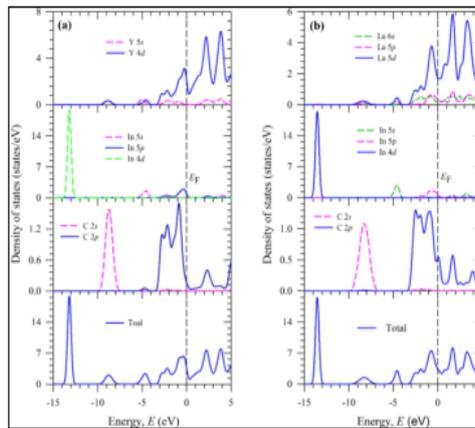


Fig 3: Calculated total and partial density of states (a) Y3InC and (b) La3InC

3.5 Optical Characteristics

The investigation of a material's optical characteristics reveals the varying behaviour of the compound depending on the field of incident light. EM radiation is a kind of electromagnetic radiation. The optical behaviour of a substance is defined as follows: The ability to operate in the visible range is critical for optoelectronic devices. Our investigation into the dielectric function was conducted in the current research. Reflectivity, refractive index, conductivity, and absorption are all terms used to describe properties of materials. The Y3InC and La3InC coefficients and loss functions are shown in the table. The dielectric function that is connected to a frequency dependent equation in mathematics, the symbol for one is equal to one plus two. The real component of this equation was acquired by solving it. The Kramers-Kronig transformation was used, as well as the relationship between ϵ_1 and ϵ_2 in ref [37], eqs. 49 to 54 are given. The second section is as follows: (imaginary part) [37] There is an additional connection between the equation and the following:

The location of the variables u and v shows the polarisation of the occurrence. The electric field and the unit cell volume, denoted by the letters e and e , are referred to as the frequency of light and the charge of an electron are both measured, and exposes the wave function of the conduction band as well as the valence band. K is the frequency of the band wave function. Due to the fact that the materials under consideration are of a metallic character, we now have (as validated by the band structure and DOS findings), Drude's word was employed (plasma frequency 3 eV and Drude's term). For the investigation of the dielectric function, damping of 0.05 eV was used [38]. The term The optical function of Y3InC and La3InC is being investigated in the current study.

The inquiry is shown here as a misplaced figure in Fig. All optical functions are proportional to the energy of the incoming photon, which is 45 eV. For a Gaussian smearing value of 0.5 eV is used in all optical computations. The real and imaginary components of the dielectric function that have been computed as seen in Fig. 4 (a). The actual portion demonstrates that it begins

with the negative number then progresses towards the positive, which signifies the Drude-like behaviour of the characters. In addition, Drude's actions implies metallic properties of Y₃InC and La₃InC are discussed. The fictitious portion begins with a positive value and decreases in the IR and visible region with time and approaches zero at a pressure of around 8 eV. This also serves as a reminder of the current examined compounds have a metallic character, and this is reflected in their composition. correspond to the energy range in which absorption is most pronounced As the refractive index decreases, the amount of photon energy decreases. The complex and real components of the refractive index have been shown in Fig. 4 is a diagram of a tetrahedron (b). Both compounds have a real portion that is almost identical, and have a zero-energy initial point The refractive index values that are constant across time Y₃InC and La₃InC have atomic weights of 6.84 and 7.83, respectively. The When it comes to the IR and visible area, the refractive index is quite high and approaches At around 9 eV, there is no energy. The fictitious portion is sometimes referred to as a complicated refractive index and measures the quantity of light that passes through it An EM radiation's absorption loss is measured in percent. The values of complicated variables The refractive index of both materials is comparable up to a certain point in energy. The energy ranges from 0 to 12.6 eV and exhibits the same highly concentrated components. More to the point, both materials produce the same quantity of electromagnetic radiation. radiations.

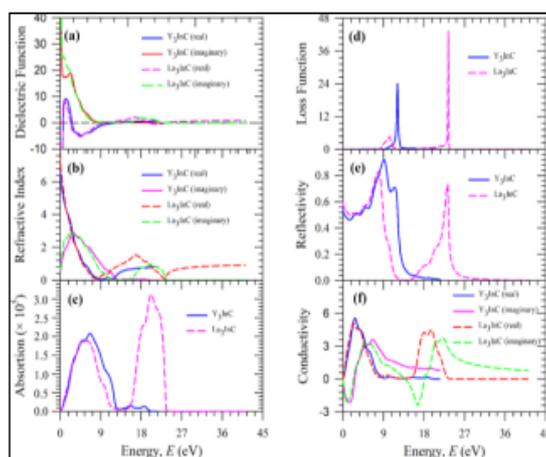


Fig 4: The frequency dependent (a) dielectric functions, (b) refractive index, (c) absorption coefficient, (d) loss function, (e) reflectivity and

The computed absorption spectra of Y₃InC and La₃InC have shown in Fig. 4 (c). From the Figure it is obvious that the absorption begins at zero energy that reveals the metallic nature. The absorbance between 0 and 12.6 eV is comparable and after 12.6 eV the impact of Y₃InC is insignificant whereas Y₃InC displays maximum absorption at 19.8 eV. The estimated loss functions were displayed in Fig. 4 (d). The loss function indicates maxima at 12.6 eV and 23.4 eV for Y₃InC and La₃InC. The energy 12.6 eV relates to the energy in whose reflectivity exhibits highest for Y₃InC and La₃InC, and La₃InC further reveals second peak at 23.4 eV. The peak energy 12.6 eV and 23.4 eV imply the bulk plasma. The maximal frequency and these spots are revealed even further. Points of energy depletion. The greater reflectivity is seen at roughly 7.2 eV and 9 eV for the first and second elements, respectively. Y₃InC and La₃InC (as illustrated in Fig. 4(e)) are examples of inorganic compounds. These are the equivalents of the amount of energy required for the conductivity to decrease to zero and the absorption quality is excellent. The La₃InC compound demonstrates excellent results. Reflectivity increases with increasing energy as well. The total reflectance of the surface. Both compounds have a similar energy range between 0 and 14.4 eV. In the case of As a result, we believe that Y₃InC and La₃InC are good candidates. substance that will be used as a reflector material for ultraviolet radiation region.

The excellent conductivity is apparent in the visible range and approximately 9 degrees Celsius. The weaker conductivity at eV has also been shown (Fig. 4(f)). The greater the score, the better. The reflectance of La₃InC has been shown to be excellent at 18 eV and above. The total conductivity value shows that the materials are good conductors of electricity. The usage of La₃InC in electrical conductors is preferable to that of La₂InC. Y₃InC is used in the visible and ultraviolet spectrums.

4. Concluding Remarks

In conclusion, a short explanation of physical qualities, including structural, mechanical, electrical, optical, and electromagnetic properties, is provided. Antiperovskites based on In have interesting thermodynamic characteristics. Physicists and engineers from across the world publish in the International Journal of Physics and Applications (IJPA). M₃InC (where M=Y and La) has been carried out with the help of the Density functional theory with plane-wave pseudo potentials is a kind of mathematical theory. The physical characteristics of these phases are being researched at the moment. at the very first time The adjusted lattice parameters demonstrate a small improvement. 1.897 percent and 2.04 percent deviations from experimental values, respectively showing that our estimations have been met with high satisfaction. The estimated elastic constants satisfy the requirement for born stability in the first place. The presence of certain circumstances shows the mechanical stability of Y₃InC as well as La₃InC. The investigation of Cauchy pressure, Pugh's ratio, and other parameters. The brittleness features of Y₃InC are shown by the Poisson's ratio, as well as La₃InC. Peierls stresses have low values, which indicates that the Dislocation movement of Y₃InC and La₃InC is expected, according to the model. The difference between Zener's anisotropy index A and unity demonstrates. The anisotropic features of these phases are discussed more below. When it comes to calculations, The values of the Mulliken bond overlap population and the Vickers bond overlap population. The hardness of both phases indicates that they are both relatively soft materials within comparison to Diamond. The lack of a band gap at Fermi's level of analysis.

The presence of band structures and high levels of DOS at the Fermi level demonstrate. The metallic behaviour of Y₃InC and La₃InC has been investigated. When it comes to calculations, The overall density of states is 3.4061 states/eV and 3.4047 states/eV, respectively. states/eV, which demonstrate the identical metallic properties characteristics. The dielectric function has very large negative values. (in the actual world) demonstrate Drude-like conduct while also suggesting Y₃InC and La₃InC have a metallic appearance. The reflectivity spectra are shown in the diagram. demonstrates that Y₃InC and La₃InC are promising as reflector materials. the presence of a substance in the ultraviolet energy region. The conductivity spectra are shown below. demonstrates that both phases are excellent conductors, but La₃InC is not greater suitability for application in the visible and ultraviolet spectrums than Y₃InC. Thermodynamic characteristics have been calculated using various methods. carried out in accordance with elastic constants. The significance of the values of The debye temperature and the minimal thermal conductivity are shown. it is possible to utilise both phases to create a thermal barrier coating (TBC). Y₃InC has a number of benefits over La₃InC, which has a number of advantages over the former. The melting temperature demonstrates that both phases have a high melting point. The melting temperature of La₃InC is higher, and it has a more convenient impact. Y₃InC has a greater tendency to melt down.

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